

Math 115

Summer 2017

Lecture 9



$A(-5, 2)$, $B(7, 4)$

① Draw \overline{AB}

② Find M

$$M\left(\frac{-5+7}{2}, \frac{2+4}{2}\right) = M(1, 3)$$

③ Find m

$$m = \frac{2-4}{-5-7} = \frac{-2}{-12} = \boxed{\frac{1}{6}}$$

④ Find d

$$\begin{aligned} d &= \sqrt{(-5-7)^2 + (2-4)^2} \\ &= \sqrt{(-12)^2 + (-2)^2} = \sqrt{148} \\ &\approx \boxed{12.1} \end{aligned}$$

$A(-3, 5)$, $B(0, 1)$ ← Y-Int

① find $M\left(\frac{-3+0}{2}, \frac{5+1}{2}\right)$
 $= M(-1.5, 3)$

② find $m = \frac{1-5}{0-(-3)} = \frac{-4}{3}$

③ find $d = \sqrt{(-3-0)^2 + (5-1)^2}$
 $= \sqrt{25}$
 $= 5$

④ find eqn of the line AB.
 $y = mx + b$
 $y = \frac{-4}{3}x + 1$

⑤ Draw, show rise & run of slope.

Graph using the intercept method:

$2x - 7y = -14$

| x | y |
|----|---|
| 0 | 2 |
| -7 | 0 |

$-7y = -2x - 14$

$y = \frac{-2}{-7}x - \frac{14}{-7}$ $y = \frac{2}{7}x + 2$

$m = \frac{2}{7}$
 Increasing

Slope-Int. form.

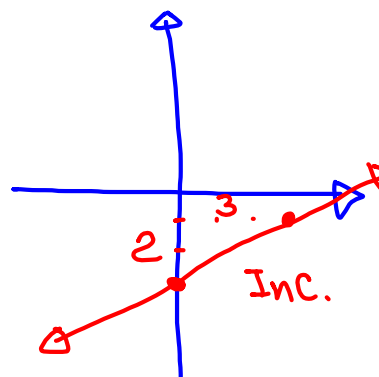
Graph using slope-Int form.

$$2x - 3y = 9 \quad y = mx + b$$

Standard form $m = \frac{2}{3}$

$$-3y = -2x + 9 \quad Y\text{-Int } (0, -3)$$

$$\boxed{y = \frac{2}{3}x - 3}$$

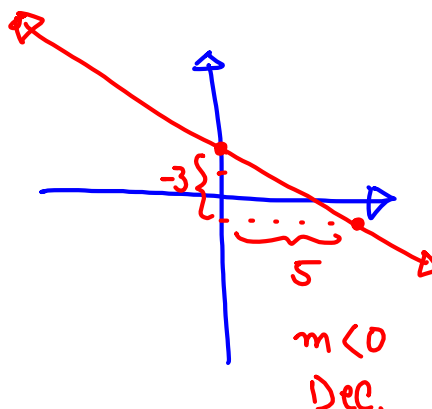


Graph using slope-Int. form

$$3x + 5y = 10.$$

$$5y = -3x + 10 \quad m = -\frac{3}{5}$$

$$y = -\frac{3}{5}x + 2 \quad Y\text{-Int } (0, 2)$$



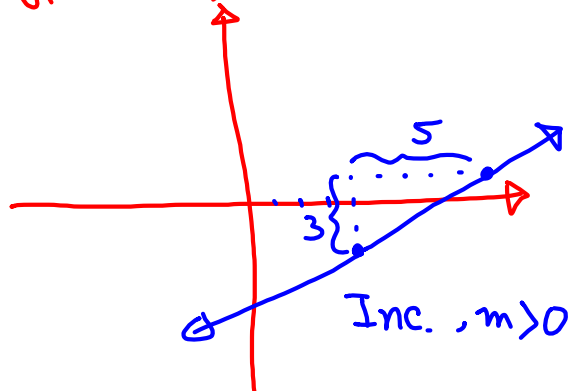
Graph using Point-Slope Form.

$$y + 2 = \frac{3}{5}(x - 4)$$

Point $(4, -2)$

Slope $\frac{3}{5}$

$$y - y_1 = m(x - x_1)$$



Graph using Point-slope.

$$y - y_1 = m(x - x_1)$$

$$y - 3 = \frac{-3}{7}(x + 4)$$

write the eqn in
slope-Int. form.

$$y - 3 = \frac{-3}{7}(x + 4)$$

$$\text{LCD} = 7$$

$$7y - 21 = -3(x + 4)$$

$$7y - 21 = -3x - 12$$

Point $(-4, 3)$

$$m = \frac{-3}{7}$$

$$7y = -3x - 12 + 21$$

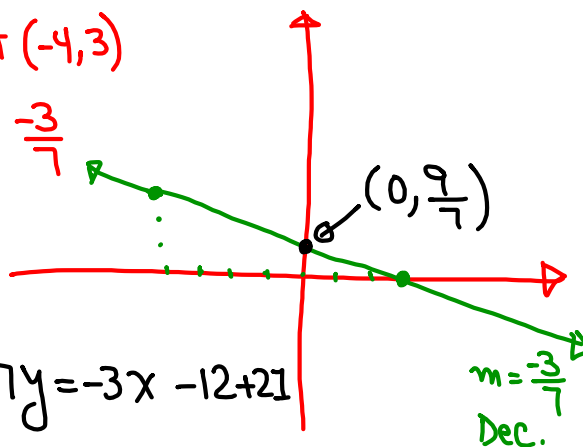
$$7y = -3x + 9$$

Isolate y

$$y = \frac{-3}{7}x + \frac{9}{7}$$

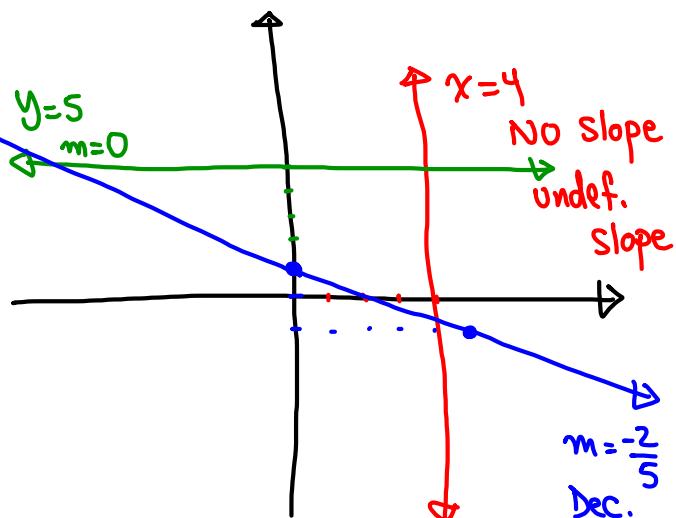
$$m = \frac{-3}{7}$$

y -Int $(0, \frac{9}{7})$



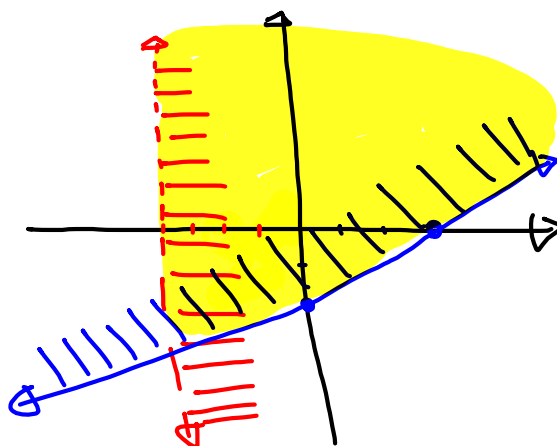
Graph

$$\begin{cases} x=4 \\ y=5 \\ y=-\frac{2}{5}x+1 \end{cases}$$



Graph & Shade:

$$\begin{cases} x > 4 \\ y \geq \frac{2}{3}x - 2 \end{cases}$$



Graph & Shade

$$\begin{cases} y \leq 3 \\ 2x - 3y < 6 \\ y > \frac{-3}{4}x - 2 \end{cases}$$

$$2x - 3y < 6$$

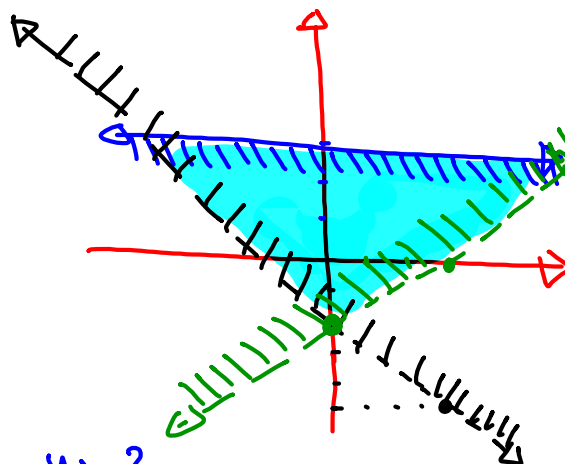
$$-3y \leq -2x + 6$$

$$\frac{-3}{-3}y > \frac{-2}{-3}x + \frac{6}{-3}$$

$$y > \frac{2}{3}x - 2$$

$$\frac{2}{3} \cdot \frac{-3}{4} = -\frac{1}{2} \neq -1$$

Hint: change 2nd line to Slope-Int. form.



Find the equation of a line that contains

(-4, 1) with slope 2.

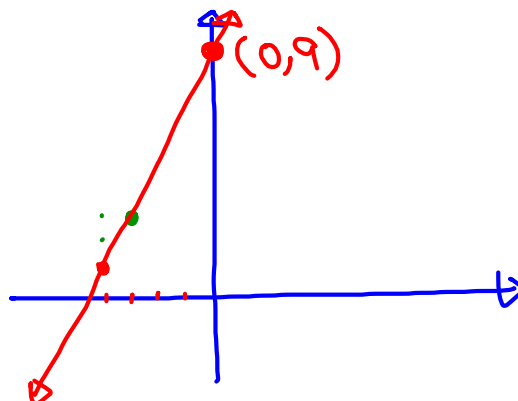
$$y - y_1 = m(x - x_1)$$

$$y - 1 = 2(x - -4)$$

Graph, show rise & run.

mark important points on the graph.

$$y = 2x + 9$$



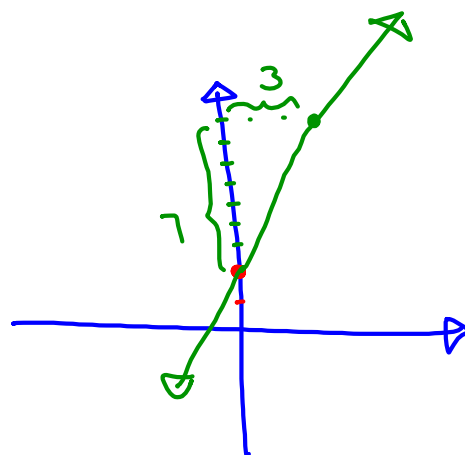
Find eqn of a line that contains $(-3, -5)$ and $(0, 2)$. Ans in Slope-Int. form. Graph, show rise & run.

$$m = \frac{-5 - 2}{-3 - 0} = \frac{-7}{-3} = \boxed{\frac{7}{3}}$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{7}{3}(x - 0)$$

$$y = \frac{7}{3}x + 2$$



Find eqn of a line that contains $(2, -3)$ and is parallel to the line $2x - 3y = -6$.
Ans in Slope-Int form.

Graph both lines.

$$(2, -3), m = \frac{2}{3}$$

$$y - y_1 = m(x - x_1)$$

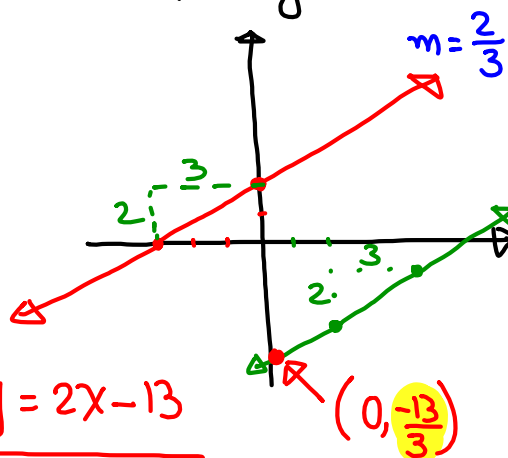
$$y + 3 = \frac{2}{3}(x - 2)$$

$$3y + 9 = 2(x - 2)$$

$$3y + 9 = 2x - 4$$

$$3y = 2x - 13$$

$$y = \frac{2}{3}x - \frac{13}{3}$$



Find eqn of a line that contains $(-4, -3)$ and is perpendicular to the line $5x + 2y = 10$.

Graph both lines.

Ans. in slope-Int form.

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = \frac{2}{5}(x - (-4))$$

$$y + 3 = \frac{2}{5}(x + 4) \quad \left\{ \begin{array}{l} 5y + 15 = 2x + 8 \\ \frac{2}{5} \cdot \frac{-5}{2} = \frac{-10}{10} = -1 \end{array} \right.$$

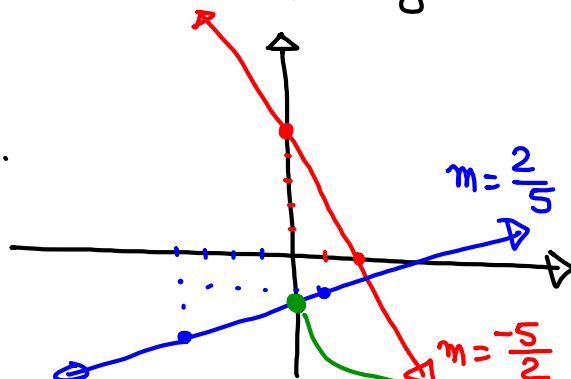
LCD = 5

$$5y + 15 = 2(x + 4)$$

$$5y = 2x - 7$$

$$y = \frac{2}{5}x - \frac{7}{5}$$

$$(0, -\frac{7}{5})$$



Find eqn of a line that contains $(5, -2)$ and

1) Zero slope

H.L.

$$y = -2$$

2) No slope

$$V.L. \quad x = 5$$

3) undefined slope

V.L.

$$x = 5$$

4) slope $\frac{2}{5}$

$$y - y_1 = m(x - x_1)$$

$$y - (-2) = \frac{2}{5}(x - 5)$$

$$y + 2 = \frac{2}{5}(x - 5)$$

$$y + 2 = \frac{2}{5}x - 2$$

$$y = \frac{2}{5}x - 4$$

Find eqn of a line that contains $(-4, 3)$ and

1) $(5, 3)$ $\boxed{y = 3}$

$$m = \frac{3-3}{5-(-4)} = 0$$

2) $(-4, -7)$ $\boxed{x = -4}$

$$m = \frac{-7-3}{-4-(-4)} = \phi$$

3) $(0, 0)$

$$m = \frac{3-0}{-4-0} = \boxed{-\frac{3}{4}}$$

$$\boxed{y = -\frac{3}{4}x}$$

4) Parallel to $y = 2x - 4$

$$y - 3 = 2(x - (-4))$$

$$\boxed{y = 2x + 11}$$

5) Perpendicular to
 $y = -\frac{2}{3}x + 1$

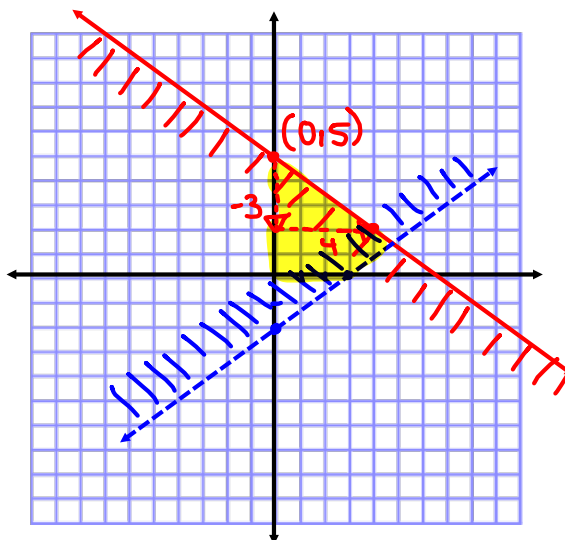
$$y - 3 = \frac{3}{2}(x + 4)$$

$$y - 3 = \frac{3}{2}x + 6$$

$$\boxed{y = \frac{3}{2}x + 9}$$

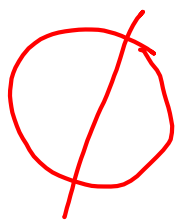
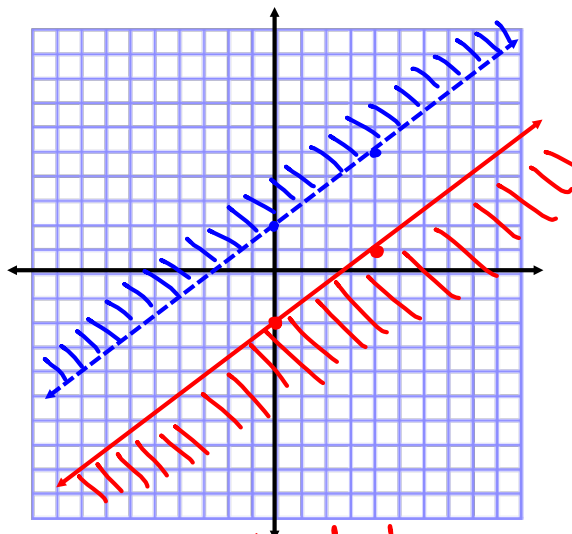
Graph & Shade

$$\begin{cases} y \leq -\frac{3}{4}x + 5 \\ y > \frac{2}{3}x - 2 \\ x \geq 0 \\ y \geq 0 \end{cases} \text{ QI}$$



Graph & Shade the Solution

$$\begin{cases} y > \frac{3}{4}x + 2 \\ y \leq \frac{3}{4}x - 2 \end{cases}$$



No Common Shaded region.

Ch. 8

Is $(-2, -4)$ a Solution of $\begin{cases} 2x - 3y = 8 \\ x - 2y = 6 \end{cases}$?

checking $2x - 3y = 8$: checking $x - 2y = 6$:

$$\begin{aligned} 2(-2) - 3(-4) &= 8 \\ -4 + 12 &= 8 \\ 8 &= 8 \checkmark \end{aligned}$$

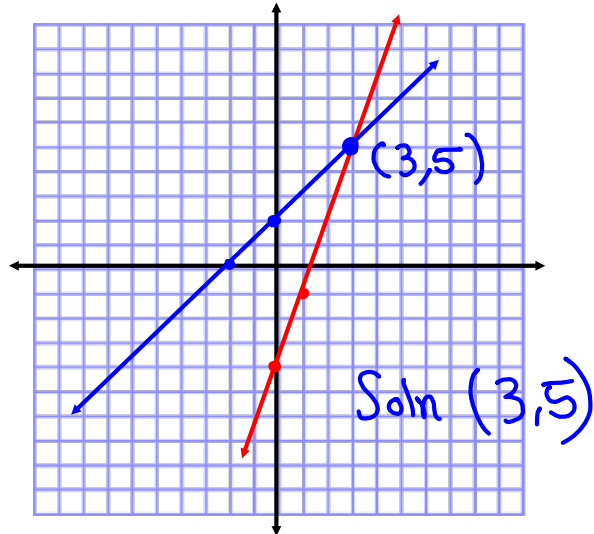
$$\begin{aligned} -2 - 2(-4) &= 6 \\ -2 + 8 &= 6 \\ 6 &= 6 \checkmark \end{aligned}$$

Yes, $(-2, -4)$ is a Solution.

Solve by Graphing method

$$\begin{cases} y = 3x - 4 \checkmark \\ x - y = -2 \checkmark \end{cases}$$

check $5 = 3(3) - 4$
 $5 = 9 - 4$
 $5 = 5$
 $3 - 5 = -2$
 $-2 = -2$



Solve by subs.

$$\begin{cases} 5y - 7x = 18 \\ y = 2x + 3 \end{cases} \Rightarrow 5(2x + 3) - 7x = 18$$

$$10x + 15 - 7x = 18$$

$$3x = 18 - 15$$

$$3x = 3$$

$$\boxed{x = 1}$$

$$y = 2(\textcolor{red}{1}) + 3$$

$$\boxed{y = 5}$$

$$(1, 5)$$

Solve by addition/elimination method:

$$-5 \begin{cases} x + 4y = 14 \\ 5x + 3y = 2 \end{cases} \Rightarrow \begin{cases} -5x - 20y = -70 \\ 5x + 3y = 2 \end{cases}$$

$$x + 4(4) = 14$$

$$\boxed{x = -2}$$

$$-17y = -68$$

$$\boxed{y = 4}$$

$$(-2, 4)$$

The sum of two numbers is 7, their difference is 3. Use system of linear eqns in two variables to find them.

$$\begin{cases} x + y = 7 \\ x - y = 3 \end{cases}$$

$$2x = 10$$

$$\boxed{x = 5}$$

$$5 + y = 7$$

$$\boxed{y = 2}$$

the two numbers are 5 & 2.

Perimeter of a rectangular garden is 36 m.
 the length is 3m longer than twice its
width. Use system of linear eqns in two
 variables to find its dimensions.



$$L = 2W + 3$$

$$2(2W + 3) + 2W = 36$$

$$4W + 6 + 2W = 36$$

$$\boxed{W = 5}$$

$$L = 2(5) + 3$$

$$\boxed{L = 13}$$

$$P = 36$$

$$\begin{cases} 2L + 2W = 36 \\ L = 2W + 3 \end{cases}$$

use Subs.
method

5m by 13m.

A first number plus twice a second number
 is 8.

Twice the first number plus the second number
 totals 25.

find both numbers. $F \rightarrow$ First # $S \rightarrow$ Second #

$$\begin{cases} F + 2S = 8 \\ 2F + S = 25 \end{cases}$$

$$\begin{cases} F + 2S = 8 \\ 2F + S = 25 \end{cases} \Rightarrow \begin{cases} -2F - 4S = -16 \\ 2F + S = 25 \end{cases}$$

$$-3S = 9 \Rightarrow \boxed{S = -3}$$

$$F + 2(-3) = 8$$

$$\boxed{F = 14}$$

$$14 \neq -3$$

John purchased 40 Stamps. He paid \$14.85. Stamps were of two kinds, 24¢ Stamps and 39¢ Stamps. use system of linear eqns in two variables to find # of each Stamps purchased.

$x \rightarrow \# \text{ of } 24 \text{ ¢ Stamps}$
 $y \rightarrow \# \text{ of } 39 \text{ ¢ Stamps}$

$$\begin{cases} x + y = 40 \\ 100 \cdot .24x + .39y = 14.85 \end{cases} \quad \begin{matrix} -24 \times \\ \hline \end{matrix} \begin{cases} x + y = 40 \\ 24x + 39y = 1485 \end{cases}$$

$$\begin{matrix} -24 \times \\ \hline \end{matrix} \begin{cases} x + y = 40 \\ 24x + 39y = 1485 \end{cases} \Rightarrow \begin{cases} -24x - 24y = -960 \\ 24x + 39y = 1485 \end{cases}$$

$$\begin{array}{rcl} & & 15y = 525 \\ & & y = 35 \end{array}$$

35 Stamps @ 39 ¢ each
 &
 5 Stamps @ 24 ¢ each

In his First NBA game, Lonzo Ball had 20 pts, No Free throws, he made 9 Shots. How many 3-pters did he make?

$$\begin{array}{l} x \rightarrow \# \text{ of 2-pters} \\ y \rightarrow \# \text{ of 3-pters} \end{array} \Rightarrow \begin{cases} x + y = 9 \\ 2x + 3y = 20 \end{cases}$$

$$\begin{cases} -2x - 2y = -18 \\ 2x + 3y = 20 \end{cases}$$

$$y = 2$$

He made
2 3-pters.

John Served 40 drinks in his shift.
Small drink \Rightarrow \$4, Large drink \Rightarrow \$6
He collected \$206 in total.

How many small drinks did he serve?

$$S \rightarrow \text{Small}, L \rightarrow \text{Large} \quad \begin{cases} S + L = 40 \\ 4S + 6L = 206 \end{cases}$$

$$\begin{cases} -6S - 6L = -240 \\ 4S + 6L = 206 \end{cases}$$

$$-2S = -34$$

$$S = 17$$

17 Small drinks

Two angles are Complementary.

one of them is 10° more than three times the other one.

Find both angles using

System of linear eqns
in two Variables.

$$\begin{cases} x + y = 90 \\ x = 3y + 10 \end{cases}$$

$$3y + 10 + y = 90$$

$$4y = 80$$

$$y = 20$$

$$x = 70$$

20° & 70°

Two angles are Supplementary.

one of them is 20° less than 4 times the other one.

Find both angles.

You must use system of
linear equations in two
Variables to get any credit.

$$\begin{cases} x + y = 180 \\ y = 4x - 20 \end{cases}$$

$$x + 4x - 20 = 180$$

$$5x = 200$$

$$x = 40$$

40° & 140°

Class QZ

① Solve by graphing: $\begin{cases} x + y = 3 \\ x - y = -1 \end{cases}$

② Solve by Sub.: $\begin{cases} x + y = 6 \\ y = -x - 4 \end{cases}$

③ Solve by addition/elimination: $\begin{cases} 6x - 3y = -15 \\ 4x - 2y = -10 \end{cases}$